## List of Contents

The contains two categories of routines which can be called by users. They are listed separately in the two sections below.

#### Fully Documented Routines

87 routines, for each of which an individual routine document is provided. These are regarded as the primary contents of the .

#### **Fundamental Support Routines**

15 comparatively simple routines which are documented in compact form in the relevant Chapter Introductions (X01, X02).

Note: all the routines in the above categories have either six-character names ending in 'F' or seven-character names ending in 'FP'.

## **Fully Documented Routines**

#### Chapter A00: Library Identification

A00AAFP Prints details of the NAG Parallel Library implementation

#### Chapter D01: Quadrature

- D01ATFP 1-d quadrature, adaptive, finite interval, allowing for badly behaved integrands
- D01AUFP 1-d quadrature, adaptive, finite interval, suitable for oscillating functions
- D01AXFP 1-d quadrature, adaptive, finite interval, weight functions  $\cos(\omega x)$  or  $\sin(\omega x)$
- D01DAFP 2-d quadrature, finite region
- D01FAFP Multi-dimensional quadrature, hyper-rectangle, adaptive
- D01GCFP Multi-dimensional quadrature, general product region, number-theoretic method

#### Chapter E04: Minimising or Maximising a Function

- E04FDFP Unconstrained minimum of a sum of squares, Gauss–Newton algorithm using function values only (easy-to-use)
- E04JBFP Minimum of a general nonlinear function with unconstrained, Gauss–Newton algorithm using function values only (easy-to-use)

#### Chapter F01: Matrix Operations and Distribution

| F01YAFP | Cyclic row block distribution routine for real sparse matrices stored in coordinate storage format |
|---------|--|
| F01YEFP | Distribution routine for real dense vectors distributed conformally to sparse matrices             |
| F01ZPFP | Gathering of a block distributed real vector used for F07 and F08 ScaLAPACK routines               |
| F01ZQFP | Real matrix generation and distribution in cyclic 2-d block fashion, used for F07 and F08          |
|         | ScaLAPACK routines   |
| F01ZRFP | Real matrix generation and distribution in block column fashion, used for F02 routines             |
| F01ZSFP | Real matrix generation and distribution in cyclic 2-d block fashion, used for F04 (Black           |
|         | Box) routines  |
| F01ZVFP | Complex matrix generation and distribution in cyclic 2-d block fashion, used for F07 and           |
|         | F08 ScaLAPACK routines   |
| F01ZWFP | Complex matrix generation and distribution in block column fashion, used for F02 routines          |
| F01ZXFP | Complex matrix generation and distribution in cyclic 2-d block fashion, used for F04 (Black        |
|         | Box) routines  |

#### Chapter F02: Eigenvalues and Eigenvectors

F02FQFPEigenvalues and eigenvectors of a real symmetric matrix, one-sided Jacobi methodF02FRFPEigenvalues and eigenvectors of a complex Hermitian matrix, one-sided Jacobi methodF02WQFPSingular Value Decomposition (SVD) of a real matrix, one-sided Jacobi method

F02WRFP Singular Value Decomposition (SVD) of a complex matrix, one-sided Jacobi method

#### Chapter F04: Simultaneous Linear Equations

- F04EBFP Solution of real simultaneous linear equations with multiple right-hand sides (Black Box)
- F04ECFP Solution of complex simultaneous linear equations with multiple right-hand sides (Black Box)
- F04FBFP Solution of real symmetric positive-definite simultaneous linear equations with multiple right-hand sides (Black Box)
- F04FCFP Solution of complex Hermitian positive-definite simultaneous linear equations with multiple right-hand sides (Black Box)
- F04GBFP Solution of a real linear least-squares problem multiple right-hand sides (Black Box)

### Chapter F07: Linear Equations (ScaLAPACK)

- F07ADFP LU factorization of a real general matrix (PDGETRF)
- F07AEFP Solution of a real system of linear equations, multiple right-hand sides, matrix already factorized by F07ADFP (PDGETRF)
- F07ARFP LU factorization of a complex general matrix (PZGETRF)
- F07ASFP Solution of a complex system of linear equations, multiple right-hand sides, matrix already factorized by F07ARFP (PZGETRF)
- F07FDFP Cholesky factorization of a real symmetric positive-definite matrix (PDPOTRF)
- **F07FEFP** Solution of a real symmetric positive-definite system of linear equations, multiple right-hand sides, matrix already factorized by F07FDFP (PDPOTRF)
- F07FRFP Cholesky factorization of a complex Hermitian positive-definite matrix (PZPOTRF)
- F07FSFP Solution of a complex Hermitian positive-definite system of linear equations, multiple righthand sides, matrix already factorized by F07FRFP (PZPOTRF)
- F07TGFP Estimate the condition number of a real triangular matrix (PDTRCON)

#### Chapter F08: Least-squares Problems (ScaLAPACK)

- FO8AEFP QR factorization of a real general rectangular matrix (PDGEQRF)
- F08AFFP Form all or part of an orthogonal Q from QR factorization determined by F08AEFP (PDGEQRF)
- FO8AGFP Apply the orthogonal transformation determined by FO8AEFP (PDORMQR)
- F08ASFP QR factorization of a complex general rectangular matrix (PZGEQRF)
- FO8ATFP Form all or part of a unitary Q from QR factorization determined by F08ASFP (PZGEQRF)
- F08AUFP Apply the unitary transformation determined by F08ASFP (PZUNMQR)
- F08FEFP Orthogonal reduction of a real symmetric matrix to tridiagonal form (PDSYTRD)
- F08JJFP All or selected eigenvalues of a real symmetric tridiagonal matrix by bisection (PDSTEBZ)

### Chapter F11: Sparse Linear Algebra

- F11BAFP Set-up for F11BBFP and F11BCFP, iterative solution of real (unsymmetric) system of simultaneous linear equations, Restarted Generalised Minimal Residual method (RGMRES)
  F11BBFP Main solver, iterative solution of a general (unsymmetric) system of simultaneous linear equations, Restarted Generalised Minimal Residual method (RGMRES)
- F11BCFP Information about the computations carried out by F11BBFP, iterative solution of a general (unsymmetric) system of simultaneous linear equations, Restarted Generalised Minimal Residual method (RGMRES)
- $\label{eq:F11DAFP} F11DAFP \qquad \mbox{Incomplete } LU \mbox{ factorization of the local diagonal blocks of a real sparse matrix, represented in coordinate storage format, distributed on a logical grid of processors in cyclic row block form \\ \end{tabular}$
- F11DBFP Solution of real system of linear equations, involving a real block diagonal sparse matrix, represented in coordinate storage format, distributed on a logical grid of processors in cyclic row block form
- F11DCFP Black-box routine for sparse system of linear equations
- F11GAFPSet-up for F11GBFP and F11GCFP, iterative solution of a symmetric system of simultaneous<br/>linear equations, Conjugate Gradient method or a Lanczos method based on SYMMLQ
- F11GBFP Main solver, iterative solution of a symmetric system of simultaneous linear equations, Conjugate Gradient method or a Lanczos method based on SYMMLQ
- F11GCFP Information about the computations carried out by F11GBFP, iterative solution of a symmetric system of simultaneous linear equations, Conjugate Gradient method or a Lanczos method based on SYMMLQ
- F11XAFP Set-up for F11XBFP, matrix-vector or transposed matrix-vector product involving a real sparse matrix, represented in coordinate storage format, distributed on a logical grid of processors in cyclic row block form
- F11XBFP Computes a matrix-vector or transposed matrix-vector product involving a real sparse matrix, represented in coordinate storage format, distributed on a logical grid of processors in cyclic row block form
- F11ZAFP General set-up routine for real sparse matrices, represented in coordinate storage format, distributed on a logical grid of processors in cyclic row block form

### Chapter G05: Random Number Generators

G05AAFPPseudo-random real numbers, uniform distribution over (0, 1), Wichmann-Hill generatorG05ABFPSelect a random number generator and initialise seeds to give repeatable sequence

# Chapter X04: Input/Output Utilities

| X04AAF    | Returns or sets a unit number for error message   |
|-----------|---|
| X04ABF    | Returns or sets a unit number for advisory messages   |
| X04BCFP   | Reads a real general matrix from an external file (stored in its natural, non-distributed form)                   |
|           | into an array in a cyclic 2-d block distribution on 2-d logical processor grid, used for the                      |
|           | F07 and F08 ScaLAPACK routines  |
| X04BDFP   | Outputs a real general matrix stored in a cyclic 2-d block distribution on a 2-d logical                          |
|           | processor grid to an external file (in its natural, non-distributed form), used with the F07                      |
|           | and F08 ScaLAPACK routines  |
| X04BFFP   | Outputs a set of real general matrices distributed on a 2-d logical processor grid, used with                     |
|           | the F02 routines  |
| X04BGFP   | Reads a general real matrix from an external file (stored in its natural, non-distributed form)                   |
|           | into an array in a cyclic 2-d block distribution on a 2-d logical processor grid, used for the                    |
|           | F04 (Black Box) routines  |
| X04BHFP   | Outputs a general real matrix stored in a cyclic 2-d block distribution on a 2-d logical                          |
|           | processor grid to an external file (in its natural, non-distributed form), used with the F04                      |
|           | (Black Box) routines  |
| X04BRFP   | Reads a complex general matrix from an external file (stored in its natural, non-distributed                      |
|           | form) into an array in a cyclic 2-d block distribution on 2-d logical processor grid, used for                    |
|           | the F07 and F08 ScaLAPACK routines  |
| X04BSFP   | Outputs a complex general matrix stored in a cyclic 2-d block distribution on a 2-d logical                       |
|           | processor grid to an external file (in its natural, non-distributed form), used with the F07                      |
| VADUED    | and F08 ScaLAPACK routines  |
| X04BUFP   | Outputs a set of complex general matrices distributed on a 2-d logical processor grid, used with the F02 routines |
| X04BVFP   | Reads a general complex matrix from an external file (stored in its natural, non-distributed                      |
| XU4DVFF   | form) into an array in a cyclic 2-d block distribution on a 2-d logical processor grid, used                      |
|           | for the F04 (Black Box) routines  |
| X04BWFP   | Outputs a general complex matrix stored in a cyclic 2-d block distribution on a 2-d logical                       |
| NO IDWI I | processor grid to an external file (in its natural, non-distributed form), used with the F04                      |
|           | (Black Box) routines  |
| X04YAFP   | Outputs a real dense vector, distributed conformally to a sparse matrix on a logical grid of                      |
|           | processors, to an external file   |
|           |   |

### Chapter Z01: Library Utilities

| Z01AAFP<br>Z01ABFP | Defines a 2-d logical processor grid (Library Grid) and returns the BLACS context<br>Undefines the logical processor grid and invalidates the BLACS context initialised by<br>Z01AAFP |
|--------------------|---|
| Z01ACFP            | Root processor identifier   |
| Z01ADFP            | Used in creating processes outside the default library mechanism, allows multigridding, used  |
|                    | in more advanced applications (PVM-based version only)  |
| Z01AEFP            | Used in creating processes outside the default library mechanism, allows multigridding, used  |
|                    | in more advanced applications (MPI-based version only)  |
| Z01BAFP            | Row and column indices of the root processor within the logical grid  |
| Z01BBFP            | Identifies logical processors in context in the 2-d grid declared by Z01AAFP  |
| Z01BDFP            | Information about PVM tasks (PVM-based version only)  |
| Z01BEFP            | Topology to be used by BLACS for broadcasting and global operations   |
| Z01BFFP            | Enables debugging (PVM-based version only)  |
| Z01BGFP            | Information about MPI tasks (MPI-based version only)  |
| Z01CAFP            | Number of rows or columns of a matrix held locally on a given processor when the matrix   |
|                    | is distributed in the cyclic 2-d block fashion (NUMROC)   |
| Z01CBFP            | Length of the workspace for F08AEFP and F08AFFP   |
| Z01CCFP            | Length of the workspace for F08AGFP   |

- Z01CDFP Process coordinate which possesses the entry of a distributed matrix specified by a global index (INDXG2P)
- Z01CEFP Length of the workspace for F08FEFP (PDSYTRD)

# **Fundamental Support Routines**

## Chapter X01: Mathematical Constants

#### Chapter X02: Machine Constants

| X02AHF | Largest permissible argument for sin and cos                   |
|--------|--|
| X02AJF | Machine precision  |
| X02AKF | Smallest positive model number                                 |
| X02ALF | Largest positive model number                                  |
| X02AMF | Safe range of real floating-point arithmetic                   |
| X02ANF | Safe range of complex floating-point arithmetic                |
| X02BBF | Largest representable integer                                  |
| X02BEF | Maximum number of decimal digits that can be represented       |
| X02BHF | Parameter of floating-point arithmetic model, $b$              |
| X02BJF | Parameter of floating-point arithmetic model, $p$              |
| X02BKF | Parameter of floating-point arithmetic model, $e_{\min}$       |
| X02BLF | Parameter of floating-point arithmetic model, $e_{\text{max}}$ |
| X02DJF | Parameter of floating-point arithmetic model, ROUNDS           |
|        |  |